

STAT/MA 41600  
In-Class Problem Set #31: October 24, 2018

1. Suppose that  $X$  is a continuous uniform random variable, with a constant probability density function on  $[-3, 3]$ . What is the CDF of  $X$ ?
2. Suppose  $X$  has density  $f_X(x) = 1/5$  for  $0 < x < 5$ , and  $f_X(x) = 0$  otherwise. Suppose that  $Y$  has density  $f_Y(y) = 2e^{-2y}$  for  $y > 0$ , and  $f_Y(y) = 0$  otherwise. Also suppose that  $X$  and  $Y$  are independent. Find  $P(Y > X)$ .
3. Consider three independent random variables  $X, Y, Z$  that are each uniformly distributed on the interval  $[0, 20]$ . Let  $V$  denote the minimum of these three random variables. Find the expected value of  $V$ .
4. Suppose that the pair of random variables  $X, Y$  has a constant joint probability density function on the triangle with vertices at  $(-5, 0), (5, 0), (0, 5)$ . Find the expected value of  $Y$ .