## STAT/MA 41600

## In-Class Problem Set #43: December 7, 2015

1. Suppose that the number of errors a student makes on his exam has a Poisson distribution, with an average of 3. Let X denote the number of errors.

**a.** Find the moment generating function  $M_X(t)$  of X.

**b.** Compute  $M'_X(0)$ . Hint: You should get 3 for your answer, since  $M'_X(0) = \mathbb{E}(X)$ .

**2.** Use X to denote the time (in seconds) that Mary waits for her next text to arrive. Suppose that X has an Exponential distribution, and  $\mathbb{E}(X) = 15$ .

**a.** Find the moment generating function  $M_X(t)$  of X.

**b.** Compute  $M'_X(0)$ . Hint: You should get 15 for your answer, since  $M'_X(0) = \mathbb{E}(X)$ .

**3.** Same setup as #2.

**a.** Compute  $M''_X(0)$ . This is equal to  $\mathbb{E}(X^2)$ .

**b.** Use your solutions to **2b** and **3a** to compute Var(X). Does this agree with the formula that you know, for the variance of an Exponential random variable?

**4.** Suppose that random variable X has probability mass function  $P(X = x) = (27/40)(1/3)^x$ , for integers  $0 \le x \le 3$ .

a. Verify that this is a valid probability mass function.

**b.** Manually compute the expected value of X.

c. Find the moment generating function  $M_X(t)$  of X. (If you think for a moment, it is possible to write  $M_X(t)$  without using any summation signs or addition symbols.)

**d.** Compute  $M'_X(0)$ . Hint: Your answer should agree with your answer for 4**b**.